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Computational Investigation for Life Cycle of Alumina based Induction Furnace Wall

Nirajkumar C Mehta¹, Dr. Dipesh D Shukla²

¹Ph. D. Student, Rai University, Ahmedabad, India ²Director, Amity University, Jaipur, India

Abstract— Furnaces are most commonly used for melting of materials. Induction furnaces are more beneficial as no fuel is required. It is a problem to find life cycle of Induction Melting Furnace Wall under load variation. The induction melting furnace wall is made of alumina ramming mass which is one kind of refractory material. The failure occurs due to cyclic thermal stresses due to heating and cooling cycles. Temperature distribution and thermal stress distribution fields of the induction melting furnace refractory wall were calculated by using explicit finite difference analysis based on the physical description of its failure under low cycle thermal fatigue conditions. The life span of the refractory wall is required to be found out by means of critical thermal stresses created inside the refractory wall of induction melting furnace wall from modified S - log N Curve.

Keywords— Advanced stress life analysis, Temperature distribution, Stress distribution, explicit finite difference method, Alumina ramming mass.

I. INTRODUCTION

Furnace is a term used to identify a closed space here heat is applied to a body in order to raise its temperature. The source of heat may be fuel or electricity. Commonly, metals and alloys and sometimes non-metals are heated in furnaces. The purpose of heating defines the temperature of heating and heating rate. Increase in temperature softens the metals. They become amenable to deformation. This softening occurs with or without a change in the metallic structure. Heating to lower temperatures (below the critical temperature) of the metal softens it by relieving the internal stresses. On the other hand, metals heated to temperatures above the critical temperatures leads to changes in crystal structures and recrystallization like annealing. Further some metals and alloys are melted, ceramic products vitrified, coals coked, metals like zinc are vaporized and many other processes are performed in Furnaces.

Induction furnaces are widely used in the iron industry for the casting of the different grades of cast iron products. Refractory wall of induction melting furnace is a key component which is used as insulation layer. It is made of ramming mass like silica, alumina, magnesia etc. The refractory wall is directly influenced by the thermal cycling of the high temperature molten iron in the furnace. Thermal fatigue failure is easy to happen for it because of the larger phase transformation thermal stresses and it has a shorter life. This can cause serious production accidents. Therefore, the service life problem of the refractory wall has always been a focus of attention in the application of this to the industry. (A V K Suryanarayana, Fuels Furnaces Refractory and Pyrometry).

A comprehensive literature review on computational investigation on different kinds of furnaces is done to study research trends. (Nirajkumar Mehta, May 2012). A review is done on applications of different numerical methods in heat transfer with its applications. (N C Mehta, Vipul B Gondaliya et al, February 2013). Thermal fatigue analysis of induction melting furnace wall is done for silica ramming mass. (N C Mehta, Akash D Raiyani et al, February 2013). A review is done for research on induction heating. (Vimal R Nakum et al, April 2013). A review is done for metal forming analysis using different numerical methods. (N C Mehta et al, May 2013). Transient heat transfer analysis of induction furnace is done by using finite element analysis. (Vipul Gondaliya et al, August 2013). Thermal fatigue analysis of induction furnace wall is done for alumina ramming mass. (N C Mehta et al, October 2013).

Thermal analysis of hot wall condenser is done for domestic refrigerator using numerical method for temperature distribution. (Akash D Raiyani *et al*, July 2014). Optimisation of wall thickness is done for minimum heat loss for induction furnace by finite element analysis. (Dipesh D Shukla *et al*, December 2014). A review is done on numerical analysis of furnace. (N C Mehta *et al*, April 2015). Thermal fatigue analysis of induction furnace wall is done for zirconia. (Nirajkumar C Mehta *et al*, April 2015). Comparison of finite difference method and finite element method is done for 2 D transient heat transfer problem.

(Nirajkumar Mehta *et al*, April 2015). Thermal fatigue analysis of induction furnace wall is done for magnesia ramming mass. (Nirajkumar C Mehta *et al*, June 2015). Advanced mathematical modelling of heat transfer is done for induction furnace wall of zirconia. (Nirajkumar C Mehta *et al*, December 2016). Advanced heat transfer analysis is done for alumina based refractory wall of induction furnace. (Nirajkumar Mehta *et al*, December 2016).

Here, Explicit Finite Difference Method is used to find out temperature and thermal stress variation with respect to time.

II. DEVELOPMENT OF ADVANCED EXPLICIT FINITE DIFFERENCE MODEL

We have divided Induction Furnace Wall into a Nodal Network as shown in Fig. 1. It is divided into 24 nodes. We have derived Explicit Finite Difference Equations for all nodes as per the boundary conditions applied to it. The furnace wall is having thermal conduction heat transfer between different nodes. It is having atmospheric heat convection ha applied from top side of the furnace wall which is open to atmosphere. It is having heat convection from molten metal from inside which is hi. It is having heat convection ho from cooling water which is circulating outside the furnace wall. (Yunus A Cengel, Heat and Mass Transfer).

To solve this advanced heat transfer problem of induction melting furnace wall which is made from Alumina Ramming Mass, the following initial and boundary conditions, material properties and basic assumptions are made:

Refractory Materials for induction furnace wall meets the basic assumptions in the science of mechanics.

- Environmental Temperature is homogeneous at 27° C.
- > Ignore the influence of heat radiation.
- > Ignore the effect of gravity field.
- The surface of induction melting furnace wall is clean.
- ➤ The initial temperature of the induction melting furnace is set 27° C and it is agreement with the ambient temperature during solving the problem.
- Heat convections are considered constant for this analysis.
- Scarp material input inside furnace is considered uniform for our analysis.

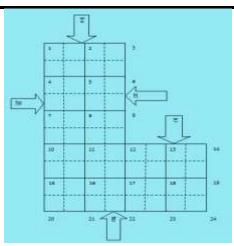


Fig.1: Nodal network for finite difference method

Node 1:

$$\begin{split} ha\frac{\Delta x}{2}(T_{\infty}-T_{1}^{i}) + \ ho\frac{\Delta y}{2}(T_{\infty}-T_{1}^{i}) + \ k\frac{\Delta y}{2}\frac{T_{2}^{i}-T_{1}^{i}}{\Delta x} + \ k\frac{\Delta x}{2}\frac{T_{4}^{i}-T_{1}^{i}}{\Delta y} = \\ \rho\frac{\Delta x}{2}\frac{\Delta y}{2}C\frac{T_{1}^{i+1}-T_{1}^{i}}{\Delta t} \\ T_{1}^{i+1} &= ((ha\frac{\Delta x}{2}(T_{\infty}-T_{1}^{i}) + \ ho\frac{\Delta y}{2}(T_{\infty}-T_{1}^{i}) + \ k\frac{\Delta y}{2}\frac{T_{2}^{i}-T_{1}^{i}}{\Delta x} + \\ k\frac{\Delta x}{2}\frac{T_{4}^{i}-T_{1}^{i}}{\Delta y})\frac{4\Delta t}{\rho(\Delta x\Delta y}) + T_{1}^{i} \end{split}$$

Node 2:

$$\begin{split} ha\Delta x \, (\,T_{\infty} - T_{2}^{\,i}) \, + \, & \, k \frac{\Delta y}{2} \frac{T_{1}^{\,i} - T_{2}^{\,i}}{\Delta x} \, + \, & \, k \frac{\Delta y}{2} \frac{T_{3}^{\,i} - T_{2}^{\,i}}{\Delta x} \, + \, & \, k \, \Delta x \, \frac{T_{5}^{\,i} - T_{2}^{\,i}}{\Delta y} \, = \\ \rho \Delta x \, \frac{\Delta y}{2} \, C \frac{T_{2}^{\,i+1} - T_{2}^{\,i}}{\Delta t} \\ T_{2}^{\,i+1} \, = \, & \, ((ha\Delta x \, (\,T_{\infty} - T_{2}^{\,i}) \, + \, k \, \frac{\Delta y}{2} \frac{T_{1}^{\,i} - T_{2}^{\,i}}{\Delta x} \, + \, k \, \frac{\Delta y}{2} \frac{T_{3}^{\,i} - T_{2}^{\,i}}{\Delta x} \, + \\ k \Delta x \, \frac{T_{5}^{\,i} - T_{2}^{\,i}}{\Delta y} \, \frac{2\Delta t}{\rho(\Delta x \Delta y)} \,) + T_{2}^{\,i} \end{split}$$

Node 3:

$$\begin{split} &ha\frac{\Delta x}{2}(T_{\infty}-T_{3}^{i})+\ hi\frac{\Delta y}{2}(T_{h}-T_{3}^{i})+\ k\frac{\Delta y}{2}\frac{T_{2}^{i}-T_{3}^{i}}{\Delta x}+\ k\frac{\Delta x}{2}\frac{T_{6}^{i}-T_{3}^{i}}{\Delta y}=\\ &\rho\frac{\Delta x}{2}\frac{\Delta y}{2}C\frac{T_{3}^{i+1}-T_{3}^{i}}{\Delta t}\\ &T_{3}^{i+1}=\ ((\ ha\frac{\Delta x}{2}(T_{\infty}-T_{3}^{i})+\ hi\frac{\Delta y}{2}(T_{h}-T_{3}^{i})+\ k\frac{\Delta y}{2}\frac{T_{2}^{i}-T_{3}^{i}}{\Delta x}+\\ &k\frac{\Delta x}{2}\frac{T_{6}^{i}-T_{3}^{i}}{\Delta y})\frac{4\Delta t}{aC\Delta x\Delta y})+T_{3}^{i} \end{split}$$

Node 4:

$$ho\Delta y (T_{\infty} - T_{4}^{i}) + k \Delta y \frac{T_{5}^{i} - T_{4}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{1}^{i} - T_{4}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{7}^{i} - T_{4}^{i}}{\Delta y} = \rho \frac{\Delta x}{2} \Delta y C \frac{T_{4}^{i+4} - T_{4}^{i}}{\Delta t}$$

$$T_{4}^{i+4} = ((ho\Delta y \ (T_{\infty} - T_{4}^{i}) + k \Delta y \frac{T_{5}^{i} - T_{4}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{1}^{i} - T_{4}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{1}^{i} - T_{4}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{2}^{i} - T_{4}^{i}}{\Delta y}) + T_{4}^{i}$$

Node 6:

$$\begin{split} &hi\Delta y \; (\; T_h - T_6^i) \; + \; \mathbf{k} \; \Delta y \frac{T_2^i - T_6^i}{\Delta x} + \; \mathbf{k} \; \frac{\Delta x}{2} \frac{T_3^i - T_6^i}{\Delta y} \; + \; \mathbf{k} \; \frac{\Delta x}{2} \frac{T_9^i - T_6^i}{\Delta y} \; = \\ &\rho \; \frac{\Delta x}{2} \; \Delta y C \frac{T_6^{i+1} - T_6^i}{\Delta t} \\ &T_6^{i+1} \; = \; \; ((\; hi\Delta y \; (\; T_h - T_6^i) \; + \; \mathbf{k} \; \Delta y \frac{T_2^i - T_6^i}{\Delta x} + \; \mathbf{k} \; \frac{\Delta x}{2} \frac{T_3^i - T_6^i}{\Delta y} \; + \\ &\mathbf{k} \frac{\Delta x}{2} \frac{T_9^i - T_6^i}{\Delta y} \right) \frac{2\Delta t}{\rho C \Delta x \Delta y} \right) \; + \; T_6^i \end{split}$$

Node 7:

$$ho\Delta y (T_{\infty} - T_{7}^{i}) + k \Delta y \frac{T_{8}^{i} - T_{7}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{4}^{i} - T_{7}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{10}^{i} - T_{7}^{i}}{\Delta y} = \rho \frac{\Delta x}{2} \Delta y C \frac{T_{7}^{i+7} - T_{7}^{i}}{\Delta t}$$

$$T_{7}^{i+7} = ((ho\Delta y (T_{\infty} - T_{7}^{i}) + k \Delta y \frac{T_{8}^{i} - T_{7}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{4}^{i} - T_{7}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{10}^{i} - T_{7}^{i}}{\Delta y}) \frac{2\Delta t}{\rho(\Delta x \Delta y)} + T_{7}^{i}$$

Node 8:

$$\begin{split} & k \, \Delta y \, \frac{T_7^i - T_8^i}{\Delta x} \, + \, k \, \Delta y \, \frac{T_9^i - T_8^i}{\Delta x} \, + \, k \, \Delta x \, \frac{T_5^i - T_8^i}{\Delta y} \, + \, k \, \Delta x \, \frac{T_{11}^i - T_8^i}{\Delta y} = \\ & \rho \Delta x \Delta y \, C \, \frac{T_8^{i+1} - T_8^i}{\Delta t} \, \\ & T_8^{i+1} = \left(\left(\begin{array}{ccc} k \, \Delta y \, \frac{T_7^i - T_8^i}{\Delta x} \, + \, k \, \Delta y \, \frac{T_9^i - T_8^i}{\Delta x} \, + \, k \, \Delta x \, \frac{T_{5}^i - T_8^i}{\Delta y} \, + \\ k \Delta x \, \frac{T_{11}^i - T_8^i}{\Delta y} \right) \, \frac{\Delta t}{\sigma (\Delta x \Delta y)} \right) + \, T_8^i \end{split}$$

Node 9:

$$\begin{split} &hi\Delta y\,(\,T_h-T_9^i)\,\,+\,\,\mathbf{k}\,\Delta y\,\frac{T_8^i-T_9^i}{\Delta x}\,+\,\,\mathbf{k}\,\frac{\Delta x}{2}\,\frac{T_6^i-T_9^i}{\Delta y}\,+\,\,\mathbf{k}\,\frac{\Delta x}{2}\,\frac{T_{12}^i-T_9^i}{\Delta y}\,=\\ &\rho\,\frac{\Delta x}{2}\,\Delta y\,\mathsf{C}\,\frac{T_9^{i+1}-T_9^i}{\Delta t}\,\\ &T_9^{i+1}=\left((hi\Delta y\,\,(\,\,T_h-T_9^i)\,\,+\,\,\,\mathbf{k}\,\,\Delta y\,\frac{T_8^i-T_9^i}{\Delta x}\,+\,\,\,\mathbf{k}\,\,\frac{\Delta x}{2}\,\frac{T_6^i-T_9^i}{\Delta y}\,\,+\,\,\mathbf{k}\,\frac{\Delta x}{2}\,\frac{T_{12}^i-T_9^i}{\Delta y}\,\,)\,\frac{2\Delta t}{\rho\,\mathsf{C}\Delta x\Delta y}\,\right)\,+\,\,T_9^i \end{split}$$

Node 10:

$$\begin{aligned} ho\Delta y (T_{\infty} - T_{10}^{i}) + k\Delta y \frac{T_{11}^{i} - T_{10}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{7}^{i} - T_{10}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{15}^{i} - T_{10}^{i}}{\Delta y} = \\ \rho \frac{\Delta x}{2} \Delta y C \frac{T_{10}^{i+10} - T_{10}^{i}}{\Delta t} \\ T_{10}^{i+10} &= \left(\left(ho\Delta y \left(T_{\infty} - T_{10}^{i} \right) + k \Delta y \frac{T_{11}^{i} - T_{10}^{i}}{\Delta x} + k \frac{\Delta x}{2} \frac{T_{7}^{i} - T_{10}^{i}}{\Delta y} + k \frac{\Delta x}{2} \frac{T_{15}^{i} - T_{10}^{i}}{\Delta y} \right) \\ k \frac{\Delta x}{2} \frac{T_{15}^{i} - T_{10}^{i}}{\Delta y} \right) \frac{2\Delta t}{\rho (\Delta x \Delta y)} + T_{10}^{i} \end{aligned}$$

Node 11:

$$\begin{split} &k \, \Delta y \, \frac{T_{10}^{i} - T_{11}^{i}}{\Delta x} \, + \, k \, \Delta y \, \frac{T_{12}^{i} - T_{11}^{i}}{\Delta x} \, + \, k \, \Delta x \, \frac{T_{8}^{i} - T_{11}^{i}}{\Delta y} \, + \, k \, \Delta x \, \frac{T_{16}^{i} - T_{11}^{i}}{\Delta y} = \\ &\rho \Delta x \Delta y \, C \, \frac{T_{11}^{i+1} - T_{11}^{i}}{\Delta t} \\ &T_{11}^{i+1} \, = \, \left(\left(\begin{array}{ccc} k \, \Delta y \, \frac{T_{10}^{i} - T_{11}^{i}}{\Delta x} \, + \, k \, \Delta y \, \frac{T_{12}^{i} - T_{11}^{i}}{\Delta x} \, + \, k \, \Delta x \, \frac{T_{8}^{i} - T_{11}^{i}}{\Delta y} \, + \\ k \Delta x \, \frac{T_{16}^{i} - T_{11}^{i}}{\Delta y} \, \right) \, \frac{\Delta t}{\sigma (\Delta x \Delta y)} \, \right) \, + \, T_{11}^{i} \end{split}$$

Node 12

$$\begin{split} hi\,\frac{\Delta x}{2}\,\left(\ T_h - T_{12}^i\right) \,\,+\,\, hi\,\frac{\Delta y}{2}\,\left(\ T_h - T_{12}^i\right) + \,\,k\,\,\Delta y\,\frac{T_{11}^i - T_{12}^i}{\Delta x} \,\,+\,\\ k\,\frac{\Delta y}{2}\,\frac{T_{13}^i - T_{12}^i}{\Delta x} + k\,\frac{\Delta x}{2}\,\frac{T_{9}^i - T_{12}^i}{\Delta y} + k\,\Delta x\,\frac{T_{17}^i - T_{12}^i}{\Delta y} = \rho\,\frac{3\Delta x\Delta y}{4}\,C\,\frac{T_{12}^{i+1} - T_{12}^i}{\Delta t} \\ T_{12}^{i+1} &= \left(\left(hi\,\frac{\Delta x}{2}(T_h - T_{12}^i) + hi\,\frac{\Delta y}{2}(T_h - T_{12}^i) + k\,\Delta y\,\frac{T_{11}^i - T_{12}^i}{\Delta x} + k\,\frac{\Delta x}{2}\,\frac{T_{13}^i - T_{12}^i}{\Delta y} + k\,\Delta x\,\frac{T_{17}^i - T_{12}^i}{\Delta y}\right)\,\frac{4\Delta t}{3\rho(\Delta x\Delta y)}\right) + \,T_{12}^i \end{split}$$

Node 13:

$$\begin{split} &hi\Delta x(T_h-T_{13}^i)+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{12}^i-T_{13}^i}{\Delta x}+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{14}^i-T_{13}^i}{\Delta x}+\ \mathbf{k}\Delta x\,\frac{T_{18}^i-T_{13}^i}{\Delta y}=\\ &\rho\Delta x\frac{\Delta y}{2}\left(\frac{T_{13}^{i+1}-T_{13}^i}{\Delta t}\right)\\ &T_{13}^{i+1}=\left(\left(hi\Delta x\left(T_h-T_{13}^i\right)+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{12}^i-T_{13}^i}{\Delta x}+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{14}^i-T_{13}^i}{\Delta x}+\\ &\mathbf{k}\Delta x\,\frac{T_{18}^i-T_{13}^i}{\Delta y}\right)\frac{2\Delta t}{\rho(\Delta x\Delta y)}\right)+T_{13}^i\\ &\mathrm{Node}\ 14:\\ &hi\,\frac{\Delta x}{2}(T_h-T_{14}^i)+\ hi\,\frac{\Delta y}{2}(T_h-T_{14}^i)+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{13}^i-T_{14}^i}{\Delta x}+\ \mathbf{k}\frac{\Delta x}{2}\frac{T_{19}^i-T_{14}^i}{\Delta y}\\ &=\rho\,\frac{\Delta x}{2}\frac{\Delta y}{2}\left(\frac{T_{14}^{i+1}-T_{14}^i}{\Delta t}\right)\\ &T_{14}^{i+1}=\left(\left(hi\,\frac{\Delta x}{2}(T_h-T_{14}^i)+\ hi\,\frac{\Delta y}{2}(T_h-T_{14}^i)+\ \mathbf{k}\frac{\Delta y}{2}\frac{T_{13}^i-T_{14}^i}{\Delta x}+\\ &\mathbf{k}\frac{\Delta x}{2}\frac{T_{19}^i-T_{14}^i}{\Delta y}\right)\frac{4\Delta t}{\rho(\Delta x\Delta y)}+T_{14}^i \end{split}$$

Node 15:

$$ho\Delta y(T_{\infty} - T_{15}^{i}) + k\Delta y \frac{T_{16}^{i} - T_{15}^{i}}{\Delta x} + k\frac{\Delta x}{2} \frac{T_{10}^{i} - T_{15}^{i}}{\Delta y} + k\frac{\Delta x}{2} \frac{T_{20}^{i} - T_{15}^{i}}{\Delta y} =$$

$$\rho \frac{\Delta x}{2} \Delta y C \frac{T_{15}^{i+15} - T_{15}^{i}}{\Delta t}$$

$$T_{15}^{i+15} = ((ho\Delta y(T_{\infty} - T_{15}^{i}) + k\Delta y \frac{T_{16}^{i} - T_{15}^{i}}{\Delta x} + k\frac{\Delta x}{2} \frac{T_{10}^{i} - T_{15}^{i}}{\Delta y} + k\frac{\Delta x}{2} \frac{T_{20}^{i} - T_{15}^{i}}{\Delta y}) + T_{15}^{i}$$

Node 16:

$$\begin{split} &k\Delta y \frac{T_{15}^{i} - T_{16}^{i}}{\Delta x} + k\Delta y \frac{T_{17}^{i} - T_{16}^{i}}{\Delta x} + k\Delta x \frac{T_{11}^{i} - T_{16}^{i}}{\Delta y} + k\Delta x \frac{T_{21}^{i} - T_{16}^{i}}{\Delta y} = \\ &\rho \Delta x \Delta y C \frac{T_{16}^{i+1} - T_{16}^{i}}{\Delta t} \\ &T_{16}^{i+1} = \left(\left(k \Delta y \frac{T_{15}^{i} - T_{16}^{i}}{\Delta x} + k \Delta y \frac{T_{17}^{i} - T_{16}^{i}}{\Delta x} + k \Delta x \frac{T_{11}^{i} - T_{16}^{i}}{\Delta y} + k\Delta x \frac{T_{21}^{i} - T_{16}^{i}}{\Delta y} \right) \frac{\Delta t}{\sigma(\Delta x \Delta y)} \right) + T_{16}^{i} \end{split}$$

Node 17:

$$\begin{split} &k\,\Delta y\,\frac{T_{16}^{i}-T_{17}^{i}}{\Delta x}\,+\,k\,\Delta y\,\frac{T_{18}^{i}-T_{17}^{i}}{\Delta x}\,+\,k\,\Delta x\,\frac{T_{12}^{i}-T_{17}^{i}}{\Delta y}\,+\,k\,\Delta x\,\frac{T_{22}^{i}-T_{17}^{i}}{\Delta y} = \\ &\rho\Delta x\Delta yC\,\frac{T_{17}^{i+1}-T_{17}^{i}}{\Delta t} \\ &T_{17}^{i+1} = ((k\,\Delta y\,\frac{T_{16}^{i}-T_{17}^{i}}{\Delta x}\,+\,k\,\Delta y\,\frac{T_{18}^{i}-T_{17}^{i}}{\Delta x}\,+\,k\,\Delta x\,\frac{T_{12}^{i}-T_{17}^{i}}{\Delta y}\,+\,k\,\Delta x\,\frac{T_{22}^{i}-T_{17}^{i}}{\Delta y}) \\ &+\,k\Delta x\,\frac{T_{22}^{i}-T_{17}^{i}}{\Delta y})\,\frac{\Delta t}{\rho C\Delta x\Delta y})\,+\,T_{17}^{i} \end{split}$$

Node 18:

$$\begin{split} &k\,\Delta y\,\frac{T^{i}_{17}-T^{i}_{18}}{\Delta x}\,+\,k\,\Delta y\,\frac{T^{i}_{19}-T^{i}_{18}}{\Delta x}\,+\,k\,\Delta x\,\frac{T^{i}_{13}-T^{i}_{18}}{\Delta y}\,+\,k\,\Delta x\,\frac{T^{i}_{23}-T^{i}_{18}}{\Delta y} = \\ &\rho\Delta x\Delta yC\,\frac{T^{i+1}_{18}-T^{i}_{18}}{\Delta t}\,\\ &T^{i+1}_{18} = \left(\left(\,k\,\Delta y\,\frac{T^{i}_{17}-T^{i}_{18}}{\Delta x}\,+\,k\,\Delta y\,\frac{T^{i}_{19}-T^{i}_{18}}{\Delta x}\,+\,k\,\Delta x\,\frac{T^{i}_{13}-T^{i}_{18}}{\Delta y}\,+\,k\,\Delta x\,\frac{T^{i}_{23}-T^{i}_{18}}{\Delta y}\,+\,k\,\Delta x\,\frac{T^{i}_{23}-T^{i}_{18}}{\Delta y}\,+\,\frac{\Delta t}{\rho(\Delta x\Delta y)}\,+\,T^{i}_{18} \end{split}$$

Node 19:

$$\begin{split} hi\Delta y (T_h - T_{19}^i) + & \ k\Delta y \frac{T_{18}^i - T_{19}^i}{\Delta x} + \ k \frac{\Delta x}{2} \frac{T_{14}^i - T_{19}^i}{\Delta y} + \ k \frac{\Delta x}{2} \frac{T_{24}^i - T_{19}^i}{\Delta y} = \\ & \rho \frac{\Delta x}{2} \Delta y C \frac{T_{19}^{i+1} - T_{19}^i}{\Delta t} \\ & T_{19}^{i+1} = \left(\left(hi\Delta y \left(T_h - T_{19}^i \right) + \ k \Delta y \frac{T_{18}^i - T_{19}^i}{\Delta x} + \ k \frac{\Delta x}{2} \frac{T_{14}^i - T_{19}^i}{\Delta y} + \right. \\ & \left. k \frac{\Delta x}{2} \frac{T_{24}^i - T_{19}^i}{\Delta y} \right) \frac{2\Delta t}{\rho (\Delta x \Delta y)} + T_{19}^i \end{split}$$

Node 20:

$$\begin{split} &ho\frac{\Delta x}{2} \left(\ T_{\infty} - T_{20}^{i} \right) + \ ho\frac{\Delta y}{2} \left(\ T_{\infty} - T_{20}^{i} \right) + \ k\frac{\Delta y}{2} \frac{T_{21}^{i} - T_{20}^{i}}{\Delta x} + \\ &k\frac{\Delta x}{2} \frac{T_{15}^{i} - T_{20}^{i}}{\Delta y} = \rho\frac{\Delta x}{2} \frac{\Delta y}{2} C \frac{T_{20}^{i+20} - T_{20}^{i}}{\Delta t} \\ &T_{20}^{i+20} = \left(\left(ho\frac{\Delta x}{2} \ \left(\ T_{\infty} - T_{20}^{i} \right) + ho\frac{\Delta y}{2} \ \left(\ T_{\infty} - T_{20}^{i} \right) + \\ &k\frac{\Delta y}{2} \frac{T_{21}^{i} - T_{20}^{i}}{\Delta x} + k\frac{\Delta x}{2} \frac{T_{15}^{i} - T_{20}^{i}}{\Delta y} \right) \frac{4\Delta t}{\rho C \Delta x \Delta y} \right) + T_{20}^{i} \end{split}$$

Node 21:

$$\begin{aligned} ho\Delta x (T_{\infty} - T_{21}^{i}) + & \ k\frac{\Delta y}{2} \frac{T_{20}^{i} - T_{21}^{i}}{\Delta x} + & \ k\frac{\Delta y}{2} \frac{T_{22}^{i} - T_{21}^{i}}{\Delta x} + & \ k\Delta x \frac{T_{16}^{i} - T_{21}^{i}}{\Delta y} = \\ \rho\Delta x \frac{\Delta y}{2} & \ (\frac{T_{21}^{i+1} - T_{21}^{i}}{\Delta t}) \end{aligned}$$

$$\begin{split} T_{21}^{i+1} &= \left(\left(ho\Delta x \left(T_{\infty} - T_{21}^{i} \right) + \ \mathbf{k} \, \frac{\Delta y}{2} \frac{T_{20}^{i} - T_{21}^{i}}{\Delta x} + \ \mathbf{k} \, \frac{\Delta y}{2} \frac{T_{22}^{i} - T_{21}^{i}}{\Delta x} + \\ \mathbf{k} \Delta x \, \frac{T_{16}^{i} - T_{21}^{i}}{\Delta y} \right) \, \frac{2\Delta t}{\rho (\Delta x \Delta y)} \right) + \, T_{21}^{i} \end{split}$$

Node 22:

$$\begin{split} &ho\Delta x(T_{\infty}-T_{22}^{i}) + \ \mathbf{k}\frac{\Delta y}{2}\frac{T_{21}^{i}-T_{22}^{i}}{\Delta x} + \ \mathbf{k}\frac{\Delta y}{2}\frac{T_{23}^{i}-T_{22}^{i}}{\Delta x} + \ \mathbf{k}\Delta x\frac{T_{17}^{i}-T_{22}^{i}}{\Delta y} = \\ &\rho\Delta x\frac{\Delta y}{2}C\frac{T_{22}^{i+1}-T_{22}^{i}}{\Delta t} \\ &T_{22}^{i+1} = \left(\left(ho\Delta x\left(T_{\infty}-T_{22}^{i}\right) + \ \mathbf{k}\frac{\Delta y}{2}\frac{T_{21}^{i}-T_{22}^{i}}{\Delta x} + \ \mathbf{k}\frac{\Delta y}{2}\frac{T_{23}^{i}-T_{22}^{i}}{\Delta x} + \\ &\mathbf{k}\Delta x\frac{T_{17}^{i}-T_{22}^{i}}{\Delta y}\right)\frac{2\Delta t}{\rho(\Delta x\Delta y)} + T_{22}^{i} \end{split}$$

Node 23:

$$\begin{split} &ho\Delta x(T_{\infty}-T_{23}^{i}) + \,\,\mathbf{k}\frac{\Delta y}{2}\frac{T_{22}^{i}-T_{23}^{i}}{\Delta x} + \,\,\mathbf{k}\frac{\Delta y}{2}\frac{T_{24}^{i}-T_{23}^{i}}{\Delta x} + \,\,\mathbf{k}\Delta x\,\frac{T_{18}^{i}-T_{23}^{i}}{\Delta y} = \\ &\rho\Delta x\,\frac{\Delta y}{2}\,\mathbf{C}\frac{T_{23}^{i+1}-T_{23}^{i}}{\Delta t} \\ &T_{23}^{i+1} = \left(\left(ho\Delta x\,(\,T_{\infty}-T_{23}^{i}) + \,\,\mathbf{k}\,\frac{\Delta y}{2}\frac{T_{22}^{i}-T_{23}^{i}}{\Delta x} + \,\,\mathbf{k}\,\frac{\Delta y}{2}\frac{T_{24}^{i}-T_{23}^{i}}{\Delta x} + \,\,\mathbf{k}\Delta x\,\frac{T_{18}^{i}-T_{23}^{i}}{\Delta x}\right) \\ &+ \,\,\mathbf{k}\Delta x\,\frac{T_{18}^{i}-T_{23}^{i}}{\Delta y}\,\frac{2\Delta t}{\sigma(\Delta x)y}\,\right) + \,\,T_{23}^{i} \end{split}$$

Node 24

$$\begin{split} &ho\frac{\Delta x}{2} \left(\ T_{\infty} - T_{24}^{i} \right) \ + \ hi\frac{\Delta y}{2} \left(\ T_{h} - T_{24}^{i} \right) \ + \ k\frac{\Delta y}{2}\frac{T_{23}^{i} - T_{24}^{i}}{\Delta x} \ + \\ &k\frac{\Delta x}{2}\frac{T_{19}^{i} - T_{24}^{i}}{\Delta y} = \rho\frac{\Delta x}{2}\frac{\Delta y}{2}C\frac{T_{24}^{i+1} - T_{24}^{i}}{\Delta t} \\ &T_{24}^{i+1} = \left(\left(ho\frac{\Delta x}{2} (T_{\infty} - T_{24}^{i}) + \ hi\frac{\Delta y}{2} (T_{h} - T_{24}^{i}) + \ k\frac{\Delta y}{2}\frac{T_{23}^{i} - T_{24}^{i}}{\Delta x} + \\ &k\frac{\Delta x}{2}\frac{T_{19}^{i} - T_{24}^{i}}{\Delta y} \right)\frac{4\Delta t}{\rho C\Delta x \Delta y} \right) + T_{24}^{i} \end{split}$$

III. PROGRAMMING & SOLUTION

With the help of a computer program we can solve the matrix created by finite difference equations for 24 nodes. We can calculate temperature distribution and stress distribution with respect to time.

Table.1: Material Property and Boundary Conditions

Material Properties and		Boundary	Unit
Con	Oilit		
1	Internal Film Co-efficient	200	W/m^2
	hi		K
2	External Film Co-efficient	40	W/m ²
	ho		K
3	Atmosphere Film Co-	10	W/m^2
	efficient ha		K
4	Density	3400	Kg/m ³
5	Time Interval Δt	10	Secon

			ds
6	Thermal Conductivity k	2.6	W/m K
7	Temperature outside Furnace Wall	303	Kelvin
8	Temperature inside Furnace Wall	1873	Kelvin
9	Temperature of Air	303	Kelvin
10	Specific Heat	920	J/kg K
11	Elasticity Constant	220000	N/m^2
12	Thermal Expansion Co- efficient	0.00000 088	m/ K
13	Ultimate Stress	500	MPa

Computer Program

cin>>c:

```
#include<iostream.h>
#include<conio.h>
#include<math.h>
#include<complex.h>
#include<fstream.h>
void main()
    clrscr;
ofstreammyfile;
myfile.open ("outputfdm.txt");
myfile << "Writing this to a file.\n";
float T[25][500];
float S[25][500];
float hi,ho,ha,To,r,t,k,Ta,c,Th,E,Af,Sut,Se,m,N,L;
cout << "Enter in W/m2 K value of hi";
cin>>hi:
cout<<"Enter in W/m2 K value of ho";
cout << "Enter in W/m2 K value of ha";
cin>>ha:
cout << "Enter in Kg/m3 value of density";
cout << "Enter in seconds time interval delta t";
cout << "Enter in W/m K value of thermal conductivity";
cout<<"Enter in Kelvin Temperature outside Furnace
Wall";
cin>>Ta;
cout<<"Enter in Kelvin Temperature inside Furnace Wall";
cout << "Enter in Kelvin Temperature of Air";
cin>>To:
cout << "Enter in J/Kg K value of Specific Heat";
```

```
cout<<"Enter in N/m2 value of Elasticity Constant";
cin>>E;
cout<<"Enter in m/K Thermal Expansion Co-efficient";</pre>
cin>>Af:
cout<<"Enter in MPA value of Ultimate Stress";
cin>>Sut:
T[1][0]=300;
T[2][0]=300;
T[3][0]=300;
T[4][0]=300;
T[5][0]=300;
T[6][0]=300;
T[7][0]=300;
T[8][0]=300;
T[9][0]=300;
T[10][0]=300;
T[11][0]=300;
T[12][0]=300;
T[13][0]=300;
T[14][0]=300;
T[15][0]=300;
T[16][0]=300;
T[17][0]=300;
T[18][0]=300;
T[19][0]=300;
T[20][0]=300;
T[21][0]=300;
T[22][0]=300;
T[23][0]=300;
T[24][0]=300;
for (inti=0; i < 270; i++)
T[1][i+1] = (((0.5*ha*0.06*(To-T[1][i])) + (ho*0.3*(Ta-ta-ta)))
T[1][i]/2+(0.5*k*0.3*(T[2][i]-
T[1][i])/0.06)+(0.5*k*0.06*(T[4][i]-T[1][i])/0.3)
*((4*t)/(r*c*0.06*0.3))+T[1][i];
T[2][i+1] = (((ha*0.06*(To-T[2][i]))+(0.5*k*0.3*(T[1][i]-
T[2][i]/0.06+(0.5*k*0.3*(T[3][i]-T[2][i])/0.06)
+(0.5*k*0.06*(T[5][i]-
T[2][i]/0.3)*((2*t)/(r*c*0.06*0.3))+T[2][i];
T[3][i+1] = (((ha*0.06*(To-T[3][i])*0.5) + (hi*0.3*(Th-I)))
                                     +(0.5*k*0.3*(T[2][i]-
T[3][i])*0.5
                       )
T[3][i]/0.06)+(0.5*k*0.06*(T[6][i]-T[3][i])/0.3))
*((4*t)/(r*c*0.06*0.3)))+T[3][i];
T[4][i+1] = (((ho*0.3*(Ta-T[4][i])) +(k*0.3*(T[5][i]-
T[4][i]/0.06)+(0.5*k*0.06*(T[1][i]-T[4][i])/0.3)
(0.5*k*0.06*(T[7][i]-T[4][i])/0.3))
*((2*t)/(r*c*0.06*0.3)))+T[4][i];
```

```
T[5][i+1]
                                                                                 (((k*0.3*(T[4][i]-
                                                                                                                                    T[16][i+1]
                                                                                                                                                                                    (k*0.06*(T[15][i]-T[16][i])/0.06)+
                                                                                                                                                                          ((
T[5][i]/0.06)+(k*0.3*(T[6][i]-T[5][i])/0.06)
                                                                                                                                     (k*0.06*(T[17][i]-T[16][i])/0.06
                                                                                                                                                                                                               )+(k*0.06*(T[11][i]-
(k*0.06*(T[8][i]-T[5][i])/0.3))
                                                                                                                                    T[16][i])/0.06)+(
                                                                                                                                                                                       k*0.06*(T[21][i]-T[16][i])/0.06))
                                                                                                                                     *((t)/(r*c*0.06*0.06)))+T[16][i];
*((t)/(r*c*0.06*0.3)))+T[5][i];
T[6][i+1] = (((hi*0.3*(Th-T[6][i])) + (k*0.3*(T[2][i]-
                                                                                                                                    T[17][i+1] =
                                                                                                                                                                      ((
                                                                                                                                                                                    (k*0.06*(T[16][i]-T[17][i])/0.12)+
                                                                                                                                    (k*0.06*(T[18][i]-T[17][i])/0.12
T[6][i]/0.06)+(0.5*k*0.06*(T[3][i]-T[6][i])/0.3)
                                                                                                                                                                                                               +(k*0.12*(T[12][i]-
(0.5*k*0.06*(T[9][i]-T[6][i])/0.3))
                                                                                                                                    T[17][i])/0.06)+(
                                                                                                                                                                                       k*0.12*(T[22][i]-T[17][i])/0.06))
*((2*t)/(r*c*0.06*0.3)))+T[6][i];
                                                                                                                                     *((t)/(r*c*0.12*0.06)))+T[17][i];
T[7][i+1] = (((ho*0.3*(Ta-T[7][i])) + (k*0.3*(T[8][i]-i)))
                                                                                                                                                             = (( (k*0.06*(T[17][i]-T[18][i])/0.18)+
                                                                                                                                    T[18][i+1]
T[7][i]/0.06)+(0.5*k*0.06*(T[4][i]-T[7][i])/0.3)
                                                                                                                                    (k*0.06*(T[19][i]-T[18][i])/0.18
                                                                                                                                                                                                               +(k*0.18*(T[13][i]-
(0.5*k*0.06*(T[10][i]-T[7][i])/0.3))
                                                                                                                                    T[18][i])/0.06)+(
                                                                                                                                                                                       k*0.18*(T[23][i]-T[18][i])/0.06))
((2*t)/(r*c*0.06*0.3))+T[7][i];
                                                                                                                                     (t)/(r*c*0.18*0.06))+T[18][i];
T[8][i+1]
                                                   (((k*0.3*(T[7][i]-T[8][i])/0.06)+(
                                                                                                                                    T[19][i+1] = (((hi*0.06*(Th-T[19][i]))+(k*0.06*(T[18][i]-
                                                                               +(k*0.06*(T[5][i]-
k*0.3*(T[9][i]-T[8][i])/0.06
                                                                                                                                    T[19][i])/0.18)+
                                                                                                                                                                           (0.5*k*0.18*(T[14][i]-T[19][i])/0.06)+(
                                                                )
T[8][i]/0.3
                                                       (k*0.06*(T[11][i]-T[8][i])/0.3))
                                                                                                                                    0.5*k*0.18*(T[24][i]-T[19][i])/0.06)
*((t)/(r*c*0.06*0.3)))+T[8][i];
                                                                                                                                     ((2*t)/(r*c*0.18*0.06))+T[19][i];
T[9][i+1] = (( (hi*0.3*(Th-T[9][i]))+(k*0.3*(T[8][i]-
                                                                                                                                    T[20][i+1]
                                                                                                                                                                               ((
                                                                                                                                                                                            (0.5*ho*0.06*(Ta-T[20][i]))+(
T[9][i])/0.06)+
                                         (0.5*k*0.06*(T[6][i]-T[9][i])/0.3)
                                                                                                                                    0.5*ho*0.06*(Ta-T[20][i]))+(0.5*k*0.06*(T[21][i]-
(0.5*k*0.06*(T[12][i]-T[9][i])/0.3))
                                                                                                                                                                                                            (0.5*k*0.06*(T[15][i]-
                                                                                                                                    T[20][i])/0.06)+
((2*t)/(r*c*0.06*0.3))+T[9][i];
                                                                                                                                    T[20][i]/0.06)*((4*t)/(r*c*0.06*0.06))+T[20][i];
T[10][i+1] = (((ho*0.18*(Ta-T[10][i]))+(k*0.18*(T[11][i]-
T[10][i])/0.06)+
                                     (0.5*k*0.06*(T[7][i]-T[10][i])/0.18) +
                                                                                                                                    T[21][i+1]
                                                                                                                                                                                                                    (0.5*ho*0.06*(Ta-
(0.5*k*0.06*(T[15][i]-T[10][i])/0.18))
                                                                                                                                    T[21][i])+(0.5*k*0.06*(T[20][i]-T[21][i])/0.06)+(
(2*t)/(r*c*0.06*0.18))+T[10][i];
                                                                                                                                    0.5*k*0.06*(T[22][i]-T[21][i])/0.06)+
                                                                                                                                                                                                                   (k*0.06*(T[16][i]-
                                                                                                                                    T[21][i]/0.06)*((2*t)/(r*c*0.06*0.06))+T[21][i];
T[11][i+1]
                       = ((
                                               (k*0.18*(T[10][i]-T[11][i])/0.06)+
                                                                                                                                    T[22][i+1]
                                                                                                                                                                                                    ((
                                                                                                                                                                                                                            (ho*0.12*(Ta-
(k*0.18*(T[12][i]-T[11][i])/0.06)+
                                                                                  (k*0.06*(T[8][i]-
                                                                                                                                    T[22][i])+(0.5*k*0.06*(T[21][i]-T[22][i])/0.12)+(
T[11][i])/0.18)
                                                  (k*0.06*(T[16][i]-T[11][i])/0.18))
                                                                                                                                    0.5*k*0.06*(T[23][i]-T[22][i])/0.12)+ (k*0.12*(T[17][i]-
*((t)/(r*c*0.06*0.18)))+T[11][i];
                                                                                                                                    T[22][i]/0.06)*((2*t)/(r*c*0.12*0.06))+T[22][i];
T[12][i+1]
                              =
                                           ((
                                                         (0.5*hi*0.12*(Th-T[12][i]))+(
                                                                                                                                    T[23][i+1]
                                                                                                                                                                             =
                                                                                                                                                                                                    ((
0.5*hi*0.18*(Th-T[12][i]))
                                                                                                                                    T[23][i])+(0.5*k*0.06*(T[22][i]-T[23][i])/0.18)+(
                                                                             +(k*0.18*(T[11][i]-
T[12][i])/0.12)+
                                                                       (0.5*k*0.18*(T[13][i]-
                                                                                                                                    0.5*k*0.06*(T[24][i]-T[23][i])/0.18)+ (k*0.18*(T[18][i]-
                                                                                                                                    T[23][i])/0.06))*((2*t)/(r*c*0.18*0.06)))+T[23][i];
T[12][i]/0.12)+(0.5*k*0.12*(T[9][i]-T[12][i])/0.18)
(k*0.12*(T[17][i]-T[12][i])/0.18))
                                                                                                                                    T[24][i+1]
                                                                                                                                                                  =
                                                                                                                                                                               ((
                                                                                                                                                                                            (0.5*ho*0.18*(Ta-T[24][i]))+(
*((4*t)/(3*r*c*0.12*0.18))) +T[12][i];
                                                                                                                                    0.5*hi*0.06*(Th-T[24][i]))
                                                                                                                                                                                                         +(0.5*k*0.06*(T[23][i]-
T[13][i+1]
                                                                                        (hi*0.18*(Th-
                                                                                                                                    T[24][i])/0.18)+
                                                                                                                                                                                                           (0.5*k*0.18*(T[19][i]-
T[13][i])+(0.5*k*0.18*(T[12][i]-T[13][i])/0.18)+
                                                                                                                                    T[24][i]/0.06)*((4*t)/(r*c*0.18*0.06))+T[24][i];
(0.5*k*0.18*(T[14][i]-T[13][i])/0.18)+ (k*0.18*(T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i
                                                                                                                                    S[14][i] = E*Af*T[14][i];
T[13][i]/0.18) *((2*t)/(r*c*0.18*0.18)))+T[13][i];
                                                                                                                                     }
T[14][i+1]
                                                                                (0.5*hi*0.18*(Th-
                                                                                                                                     for (i=271; i <= 360; i++)
                                                           ((
T[14][i])+(0.5*hi*0.18*(Th-T[14][i]))
+(0.5*k*0.18*(T[13][i]-T[14][i])/0.18)+
                                                                                                                                    hi=ha;
(0.5*k*0.18*(T[19][i]-T[14][i])/0.18))
                                                                                                                                    Th=Ta;
                                                                                                                                    T[1][i+1] \ = \ (((0.5*ha*0.06*(To-T[1][i])) \ + (ho*0.3*(Ta-ta-ta))) \ + (ho*0.3*(Ta-ta)) \ + (ho*0.3*(Ta)) \ + (ho*0.3*(Ta-ta)) \ +
((4*t)/(r*c*0.18*0.18))+T[14][i];
T[15][i+1] = (((ho*0.06*(Ta-T[15][i]))+(k*0.06*(T[16][i]-i)))
                                                                                                                                    T[1][i])/2)+(0.5*k*0.3*(T[2][i]-
                                                                                                                                    T[1][i])/0.06)+(0.5*k*0.06*(T[4][i]-T[1][i])/0.3)
T[15][i])/0.06)+
                                      (0.5*k*0.06*(T[10][i]-T[15][i])/0.06)+(
0.5*k*0.06*(T[20][i]-T[15][i])/0.06))
                                                                                                                                    )*((4*t)/(r*c*0.06*0.3)))+T[1][i];
(2*t)/(r*c*0.06*0.06))+T[15][i];
                                                                                                                                    T[2][i+1] = (((ha*0.06*(To-T[2][i]))+(0.5*k*0.3*(T[1][i]-
                                                                                                                                    T[2][i]/0.06)+(0.5*k*0.3*(T[3][i]-T[2][i])/0.06)
```

```
(0.5*hi*0.18*(Th-
+(0.5*k*0.06*(T[5][i]-
                                                                                                                                  T[14][i+1]
                                                                                                                                                                                            ((
T[2][i]/0.3)*((2*t)/(r*c*0.06*0.3))+T[2][i];
                                                                                                                                  T[14][i])+(0.5*hi*0.18*(Th-T[14][i]))
T[3][i+1] = (((ha*0.06*(To-T[3][i])*0.5) + (hi*0.3*(Th-I)))
                                                                                                                                  +(0.5*k*0.18*(T[13][i]-T[14][i])/0.18)+
T[3][i])*0.5
                                                                        +(0.5*k*0.3*(T[2][i]-
                                                                                                                                   (0.5*k*0.18*(T[19][i]-T[14][i])/0.18))
                                              )
                                                                                                                                   *((4*t)/(r*c*0.18*0.18)))+T[14][i];
T[3][i]/0.06)+(0.5*k*0.06*(T[6][i]-T[3][i])/0.3))
*((4*t)/(r*c*0.06*0.3)))+T[3][i];
                                                                                                                                  T[15][i+1] = (((ho*0.06*(Ta-T[15][i]))+(k*0.06*(T[16][i]-
T[4][i+1] = (((ho*0.3*(Ta-T[4][i])) +(k*0.3*(T[5][i]-
                                                                                                                                                                        (0.5*k*0.06*(T[10][i]-T[15][i])/0.06)+(
                                                                                                                                  T[15][i])/0.06)+
T[4][i]/0.06+(0.5*k*0.06*(T[1][i]-T[4][i])/0.3)
                                                                                                                                  0.5*k*0.06*(T[20][i]-T[15][i])/0.06)
(0.5*k*0.06*(T[7][i]-T[4][i])/0.3))
                                                                                                                                   ((2*t)/(r*c*0.06*0.06))+T[15][i];
((2*t)/(r*c*0.06*0.3))+T[4][i];
                                                                                                                                                                                  (k*0.06*(T[15][i]-T[16][i])/0.06)+
                                                                                                                                  T[16][i+1]
                                                                                                                                                           =
                                                                                                                                                                        ((
T[5][i+1]
                                                                                (((k*0.3*(T[4][i]-
                                                                                                                                  (k*0.06*(T[17][i]-T[16][i])/0.06
                                                                                                                                                                                                             )+(k*0.06*(T[11][i]-
T[5][i])/0.06) + (k*0.3*(T[6][i]-T[5][i])/0.06)
                                                                                                                                  T[16][i])/0.06)+(
                                                                                                                                                                                     k*0.06*(T[21][i]-T[16][i])/0.06))
(k*0.06*(T[8][i]-T[5][i])/0.3))
                                                                                                                                   *((t)/(r*c*0.06*0.06)))+T[16][i];
*((t)/(r*c*0.06*0.3)))+T[5][i];
T[6][i+1] = (((hi*0.3*(Th-T[6][i])) + (k*0.3*(T[2][i]-
                                                                                                                                  T[17][i+1]
                                                                                                                                                                        ((
                                                                                                                                                                                  (k*0.06*(T[16][i]-T[17][i])/0.12)+
T[6][i]/0.06)+(0.5*k*0.06*(T[3][i]-T[6][i])/0.3)
                                                                                                                                   (k*0.06*(T[18][i]-T[17][i])/0.12
                                                                                                                                                                                                             +(k*0.12*(T[12][i]-
(0.5*k*0.06*(T[9][i]-T[6][i])/0.3))
                                                                                                                                  T[17][i])/0.06)+(
                                                                                                                                                                                     k*0.12*(T[22][i]\text{-}T[17][i])/0.06))
*((2*t)/(r*c*0.06*0.3)))+T[6][i];
                                                                                                                                   *((t)/(r*c*0.12*0.06)))+T[17][i];
T[7][i+1] = (((ho*0.3*(Ta-T[7][i])) + (k*0.3*(T[8][i]-
                                                                                                                                                                                  (k*0.06*(T[17][i]-T[18][i])/0.18)+
                                                                                                                                  T[18][i+1] = ((
T[7][i])/0.06) + (0.5*k*0.06*(T[4][i]-T[7][i])/0.3)
                                                                                                                                   (k*0.06*(T[19][i]-T[18][i])/0.18
                                                                                                                                                                                                             )+(k*0.18*(T[13][i]-
                                                                                                                                  T[18][i])/0.06)+(
                                                                                                                                                                                     k*0.18*(T[23][i]-T[18][i])/0.06))
(0.5*k*0.06*(T[10][i]-T[7][i])/0.3))
                                                                                                                                   *((t)/(r*c*0.18*0.06)))+T[18][i];
*((2*t)/(r*c*0.06*0.3)))+T[7][i];
                                                                                                                                  T[19][i+1] = (((hi*0.06*(Th-T[19][i]))+(k*0.06*(T[18][i]-
T[8][i+1]
                                                  (((k*0.3*(T[7][i]-T[8][i])/0.06)+(
k*0.3*(T[9][i]-T[8][i])/0.06
                                                                )
                                                                              +(k*0.06*(T[5][i]-
                                                                                                                                  T[19][i])/0.18)+
                                                                                                                                                                        (0.5*k*0.18*(T[14][i]-T[19][i])/0.06)+(
T[8][i]/0.3
                                                      (k*0.06*(T[11][i]-T[8][i])/0.3))
                                                                                                                                  0.5*k*0.18*(T[24][i]-T[19][i])/0.06))
*((t)/(r*c*0.06*0.3)))+T[8][i];
                                                                                                                                   *((2*t)/(r*c*0.18*0.06)))+T[19][i];
T[9][i+1] = (( (hi*0.3*(Th-T[9][i]))+(k*0.3*(T[8][i]-
                                                                                                                                  T[20][i+1]
                                                                                                                                                                             ((
                                                                                                                                                                                          (0.5*ho*0.06*(Ta-T[20][i]))+(
T[9][i])/0.06)+
                                        (0.5*k*0.06*(T[6][i]-T[9][i])/0.3)
                                                                                                                                  0.5*ho*0.06*(Ta-T[20][i]))+(0.5*k*0.06*(T[21][i]-
(0.5*k*0.06*(T[12][i]-T[9][i])/0.3))
                                                                                                                                  T[20][i])/0.06)+
                                                                                                                                                                                                         (0.5*k*0.06*(T[15][i]-
                                                                                                                                  T[20][i])/0.06))*((4*t)/(r*c*0.06*0.06)))+T[20][i];
*((2*t)/(r*c*0.06*0.3)))+T[9][i];
T[10][i+1] = (((ho*0.18*(Ta-T[10][i]))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0.18*(T[11][i]-ta))+(k*0
                                                                                                                                  T[21][i+1]
                                                                                                                                                                                                                 (0.5*ho*0.06*(Ta-
                                                                                                                                                                                            ((
T[10][i])/0.06)+
                                      (0.5*k*0.06*(T[7][i]-T[10][i])/0.18) \ +
                                                                                                                                  T[21][i])+(0.5*k*0.06*(T[20][i]-T[21][i])/0.06)+(
(0.5*k*0.06*(T[15][i]-T[10][i])/0.18))
                                                                                                                                  0.5*k*0.06*(T[22][i]-T[21][i])/0.06)+ (k*0.06*(T[16][i]-
((2*t)/(r*c*0.06*0.18))+T[10][i];
                                                                                                                                  T[21][i]/0.06)*((2*t)/(r*c*0.06*0.06))+T[21][i];
                                                                                                                                  T[22][i+1]
T[11][i+1] = (( (k*0.18*(T[10][i]-T[11][i])/0.06)+
                                                                                                                                                                                                                         (ho*0.12*(Ta-
                                                                                                                                                                                                 ((
(k*0.18*(T[12][i]-T[11][i])/0.06)+
                                                                                (k*0.06*(T[8][i]-
                                                                                                                                  T[22][i]))+(0.5*k*0.06*(T[21][i]-T[22][i])/0.12)+(
T[11][i])/0.18)
                                                 (k*0.06*(T[16][i]-T[11][i])/0.18))
                                                                                                                                  0.5*k*0.06*(T[23][i]-T[22][i])/0.12)+ (k*0.12*(T[17][i]-1)
*((t)/(r*c*0.06*0.18)))+T[11][i];
                                                                                                                                  T[22][i]/0.06)*((2*t)/(r*c*0.12*0.06))+T[22][i];
T[12][i+1]
                                           ((
                                                        (0.5*hi*0.12*(Th-T[12][i]))+(
                                                                                                                                  T[23][i+1]
                                                                                                                                                                                                 ((
                                                                                                                                                                                                                         (ho*0.18*(Ta-
0.5*hi*0.18*(Th-T[12][i]))
                                                                            +(k*0.18*(T[11][i]-
                                                                                                                                  T[23][i])+(0.5*k*0.06*(T[22][i]-T[23][i])/0.18)+(
T[12][i])/0.12)+
                                                                      (0.5*k*0.18*(T[13][i]-
                                                                                                                                  0.5*k*0.06*(T[24][i]-T[23][i])/0.18)+ (k*0.18*(T[18][i]-
T[12][i]/0.12)+(0.5*k*0.12*(T[9][i]-T[12][i])/0.18)
                                                                                                                                  T[23][i]/0.06)*((2*t)/(r*c*0.18*0.06))+T[23][i];
(k*0.12*(T[17][i]-T[12][i])/0.18))
                                                                                                                                                                                          (0.5*ho*0.18*(Ta-T[24][i]))+(
                                                                                                                                  T[24][i+1]
                                                                                                                                                                =
                                                                                                                                                                             ((
                                                                                                                                  0.5*hi*0.06*(Th-T[24][i]))
((4*t)/(3*r*c*0.12*0.18))) +T[12][i];
                                                                                                                                                                                                      +(0.5*k*0.06*(T[23][i]-
                                                                                       (hi*0.18*(Th-
                                                                                                                                  T[24][i])/0.18)+
                                                                                                                                                                                                         (0.5*k*0.18*(T[19][i]-
T[13][i+1]
                                                               ((
T[13][i])+(0.5*k*0.18*(T[12][i]-T[13][i])/0.18)+
                                                                                                                                  T[24][i]/0.06)*((4*t)/(r*c*0.18*0.06))+T[24][i];
(0.5*k*0.18*(T[14][i]-T[13][i])/0.18)+ (k*0.18*(T[18][i]-T[13][i])/0.18)+ (k*0.18*(T[18][i]-T[13][i])/0.18)+ (k*0.18*(T[18][i]-T[13][i])/0.18)+ (k*0.18*(T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T[18][i]-T
                                                                                                                                  S[14][i] = E*Af*T[14][i];
T[13][i]/0.18) *((2*t)/(r*c*0.18*0.18)))+T[13][i];
                                                                                                                                   for(i=0; i<=360;i=i+6)
```

```
AFTER
myfile << "MAXIMUM
                          TEMPERATURE
"<<i/6<<" MINUTES"<<T[14][i]<<" KELVIN"<<endl;
                                             "<<i/i/6<<"
myfile << "MAXIMUM STRESS AFTER
MINUTES "<<S[14][i]<<" MPa"<<endl;
for(i=0; i <= 300; i++)
if (i==270)
myfile << "S" << S[14][i];
Se=0.15*Sut;
m = (Sut-Se)/7;
N = 7 - ((S[14][i]-Se)/m);
L = pow(10,N);
myfile << "N" << N;
myfile << "LIFE CYCLE" << L;
myfile.close();
}
}
getch(); }
```

IV. RESULTS AND DISCUSSION

We can see from the Fig. 2 that maximum temperature is increasing from atmospheric temperature 300 K and reaches to maximum temperature 1787 K in 45 minutes and then starts reducing and reaches to 869 K in next 15 minutes. It again starts increasing and reaches to maximum 1787 K after 105 minutes and again starts reducing. There are 10 similar temperature cycles in one day.

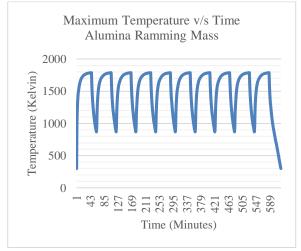


Fig.2: Maximum temperature v/s time graph for alumina ramming mass

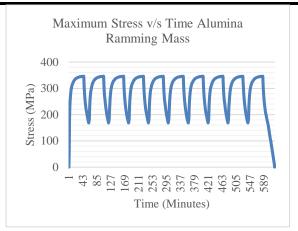


Fig.3: Maximum thermal stress v/s time graph for alumina ramming mass

We can see from the Fig. 3 that maximum thermal stress is increasing from initial condition 0 MPa and reaches to maximum stress 346 MPa in 45 minutes and then starts reducing and reaches to 168 MPa in next 15 minutes. It again starts increasing and reaches to maximum stress 346 MPa after 105 minutes and again it starts reducing. There are 10 similar thermal stress cycles in one day.

Stress-Life Method

To determine life of any component by Stress-Life Method, we need to find out ultimate strength and endurance limit of the component for the required material.

We know the values of ultimate stress for these all materials. Alumina ramming mass is having ultimate strength of 500 MPa. We can find out Se' from the equation given below or we can say dividing value of ultimate strength.

We know value of ultimate stress of alumina ramming mass is 500 Mpa.

We know the relation between Sut and Se' so that we can find out Se'.

Se' = 0.5 * Sut = 250 MPa

Endurance Limit Modifying Factors

We have seen that the rotating-beam specimen used in the laboratory to determine endurance limits is prepared very carefully and tested under closely controlled conditions.

It is unrealistic to expect the endurance limit of a mechanical or structural member to match the values obtained in the laboratory.

Some differences include

Material: composition, basis of failure, variability

Manufacturing: method, heat treatment, fretting corrosion, surface condition, stress concentration

Environment: corrosion, temperature, stress state, relaxation times

Design: size, shape, life, stress state, stress concentration, speed, fretting, galling

Marin identified factors that quantified the effects of surface condition, size, loading, temperature, and miscellaneous items. The question of whether to adjust the endurance limit by subtractive corrections or multiplicative corrections was resolved by an extensive statistical analysis of a 4340 (electric furnace, aircraft quality) steel, in which a correlation coefficient of 0.85 was found for the multiplicative form and 0.40 for the additive form.

A Marin equation is therefore written as

Se = ka*kb*kc*kd*ke*kf* Se'

Where.

ka= surface condition modification factor = 0.84

kb= size modification factor = 0.98

kc= load modification factor = 0.96

kd= temperature modification factor = 0.45

ke= reliability factor = 0.9

kf= miscellaneous-effects modification factor = 0.95

Se'= specimen endurance limit

Se = endurance limit at the critical location of a machine part in the geometry and condition of use.

We can find out different factor like surface finish factor, size factor, loading factor, temperature factor, reliability factor, miscellaneous effects factor as per the guideline. (Joseph E. Shigley*et al*, Machine Engineering Design)

Now, we can find out endurance limit for all different materials.

Se = ka*kb*kc*kd*ke*kf*Se' = 75 MPa

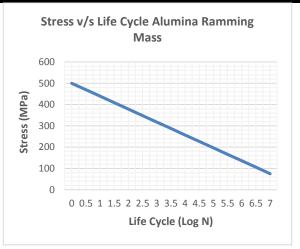


Fig. 3: Stress v/s Life Cycle for Alumina Ramming Mass

N (No. of working cycles) = $L_{min}X$ (100-Probability) / (100 X Miscellaneous Factor)

D (No. of working days) = N / (No. of working cycles per day)

Table.2: Number of Working Cycles and Number of Working Days with Probability

Sr. No.	Probability (%)	No. of working cycles for Alumina Ramming Mass	No. of days working
1	100	342	38.0
2	90	349	38.8
3	80	356	39.5
4	70	363	40.3
5	60	369	41.0
6	50	376	41.8
7	40	383	42.6
8	30	390	43.3
9	20	397	44.1
10	10	404	44.8

We can understand from this table that all cases of induction furnace wall will work for minimum 342 working cycles and 38 days. The probability will be decreasing continuously with increase in life span and working days. It happens very rarely that induction furnace wall will work for 404 working cycles and 44.8 days so its probability is minimum 10% of cases can be having such a large life span.

V. CONCLUSION

Induction Melting Furnaces are highly used now- a-days for melting of different kinds of materials. The problem comes from the alumina ramming mass of losing its material properties and failure occurs within 340-370 hours of lifetime. It will disturb production schedule as it requires time to replace the induction melting furnace wall of alumina ramming mass. Explicit finite difference analysis is done for induction melting furnace refractory wall and validation is done with respect to experimental Results. Explicit finite difference analysis is done with respect to actual working conditions of induction furnace and material properties of alumina ramming mass. Then S – log N Curves are plotted for Life Span Prediction.

We had found life span of different materials like alumina ramming mass is 340-370 cycles. From the results of experimental study and explicit finite difference analysis of thermal fatigue failure of induction melting furnace wall, it can be seen that finite difference model exactly predicts the failure of the induction furnace refractory wall and the definite solution conditions in the finite difference numerical calculation are accurate. The fatigue life of the induction melting furnace refractory wall under thermal fatigue working conditions was predicted using stress-life method by plotting S – log N curves for alumina ramming mass on the basis of explicit finite difference calculations and maximum thermal stress in the induction melting furnace refractory wall. We can use it as a linear to increase lifespan or we can use premixed alumina ramming mass for economical and better working lifespan of induction melting furnace wall.

The accuracy of the fatigue life prediction for the induction melting furnace refractory wall depends upon temperature and thermal stress spectrum calculated at the critical point by explicit finite difference method and S-log N curves prepared from the material properties and boundary condition for alumina ramming mass.

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